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### Abstract

It is shown by analysis and experimental data that constant-voltage biasing is practical with IMPATT oscillators. Constant-voltage biasing offers a lesser possibility of a thermal runaway, as compared to the conventional constant-current biasing. The price for this thermal advantage is a degradation of output power with elevating ambient temperature.

### Introduction

It is well known that in the avalanche breakdown mode, the IMPATT diode behaves very much like a zener diode; that is, as far as the bias supply is concerned, the IMPATT diode acts as a constant voltage device. For this reason a C-I (constant current) source has been traditionally used to bias IMPATT diodes for rf operations. Recently, it was reported<sup>1</sup> that an IMPATT diode operating in the amplifier mode has been successfully biased by a C-V (constant voltage) source with encouraging results. The report suggested that self-current limiting is possible with the amplifier mode but not with the oscillator mode since in the former, the diode current is limited by the finite rf power from the input. The report also claimed that by using C-V biasing, improved amplifier linearity and stability could be obtained while increasing the overall dc to rf conversion efficiency. Inspired by the report, it was decided to investigate the possibility and advantages (if any) of applying C-V bias to IMPATT amplifiers operating in the injection-locked oscillator mode.

Subsequent analysis and experiments showed that it is not only possible to use C-V biasing with IMPATT oscillators, but the combination offers a distinct advantage over the conventional C-I biasing. With C-V biasing, the IMPATT diode shows a lesser possibility of a catastrophic failure caused by thermal runaway. However, the output power decreases with elevating ambient temperature. Also, no improvement in rf performance and rf conversion efficiency was observed.

In the following sections, the thermal properties of C-I and C-V biasing will be discussed and compared. Some experimental results on C-V biasing will be presented.

### Breakdown Voltage as a Function of Temperature

For any reverse-biased semiconductor junctions, Si and GaAs included, the decreased ionization rate at high temperature gives rise to a positive temperature coefficient of breakdown voltage. A good approximation of the breakdown voltage-temperature relationship was given as<sup>2,3</sup>

$$V_b = V_{bo} (1 + \beta (T_j - T_0)) \quad (1)$$

where  $V_b$  is the device breakdown voltage at a junction temperature of  $T_j$ ,  $V_{bo}$  is the same at a reference junction temperature of  $T_0$ , and  $\beta$  is the normalized temperature coefficient defined by

$$\beta = \frac{1}{V_{bo}} \frac{dV_b}{dT_j} \quad (2)$$

Notice that the rise of the junction temperature,  $T_j$ , is caused by external heating (due to rise of the ambient temperature) and internal heating (due to power dissipation in the diode). Consider first the effect of external heating. Equation (1) can be rewritten as

$$V_b = V_{bo} + \Delta V_b; \quad \Delta V_b = \beta V_{bo} \Delta T \quad (3)$$

where  $\Delta T = T - T_0$  is the relative ambient temperature in reference to  $T_0$  and  $T$  is the ambient temperature. Equation (3) states that a change in the ambient temperature in reference to  $T_0$  introduces a change in diode breakdown voltage,  $\Delta V_b$ , in reference to  $V_{bo}$ . We shall say that  $\Delta V_b$  is caused by external heating.

When avalanche breakdown occurs, bias current flows through the device junction. In case of an IMPATT diode, only a small fraction of the bias power is converted to the rf. The remaining bias power is dissipated at the junction as heat, and as a result,  $T_j$  rises. This process causes the voltage across the diode to increase above  $V_b$  in a manner identical to external heating. We shall express the increase in diode voltage as, in analogue to Eq. (3) and with the aid of a well-known heat equation

$$\Delta V_{d1} = \beta V_{bo} \theta_t (V_d I_d + P_i - P_o) \quad (4)$$

where  $\Delta V_{d1}$  is the increase in diode voltage above  $V_b$  due to internal heating,  $\theta_t$  is the thermal resistance from the diode junction to the ambience,  $V_d$  and  $I_d$  are the bias voltage and current, respectively, of the diode,  $P_i$  is the rf injection power, and  $P_o$  is the rf output power. Furthermore, during avalanche breakdowns, the space charge of the carriers distorts the electric field profile in the space-charge layer, giving rise to a positive electrical resistance<sup>4</sup>. This so-called space-charge resistance modifies  $V_d$  in addition to  $\Delta V_{d1}$  and  $\Delta V_{d2}$ . The modification can be expressed as

$$\Delta V_{d2} = R_{sc} I_d \quad (5)$$

where  $R_{sc}$  is the space-charge resistance of the diode and can be determined experimentally<sup>2</sup>.

For the sake of closed-form solutions, we shall restrict ourselves to a first-order analysis in the next section by ignoring the terms involving  $P_i$  and  $P_o$ . (Notice that  $P_o$  is a function of  $I_d^2$ .) The error so introduced is acceptable since only a small fraction of the bias power is converted to  $P_o$ .  $\Delta V_{d1}$  is now expressed as

$$\Delta V_{d1} \approx \beta V_{bo} \theta_t V_d I_d \quad (6)$$

The total voltage across an IMPATT diode under avalanche conditions can be written as

$$V_d = V_{bo} + R_{sc} I_d + \beta V_{bo} \theta_t V_d I_d + \beta V_{bo} \Delta T \quad (7)$$

A plot of Eq. (7) is shown in Fig. 1.

### Thermal Properties of C-I and C-V Biasing

With C-I biasing,  $I_d = I_0 = \text{constant}$ , and the diode voltage as a function of temperature, by rearranging Eq. (7), can be written as

$$V_d = \frac{1}{1 - \beta \theta_t \frac{V_{bo}}{I_0}} (R_{sc} I_0 + V_{bo} + \beta V_{bo} \Delta T) \\ = a_1 + b_1 \Delta T \quad (8)$$

The junction temperature of the diode is found to be

$$T_j = \theta_t I_0 V_d + T \\ = \theta_t I_0 (a_1 + b_1 \Delta T) + \Delta T + T_0 \\ = a_2 + b_2 \Delta T \quad (9)$$

For practical cases, the parameters  $a_1$ ,  $a_2$ ,  $b_1$ ,  $b_2$  are found to be positive. It is readily seen that with C-I biasing, both diode voltage and junction temperature rise with any temperatures above  $T_0$  (i.e., for  $\Delta T > 0$ ) and that thermal runaway due to internal heating takes place if the condition  $\beta \theta_t V_{bo} I_0 = 1$  is met.

On the other hand, with C-V biasing,  $V_d = V_0 = \text{constant}$ , and the diode current and junction temperature can be shown to be

$$I_d = \frac{1}{R_{sc} + \beta \theta_t V_{bo} V_0} (V_0 - V_{bo} - \beta V_{bo} \Delta T) \\ = c_1 - d_1 \Delta T \quad \text{for } \Delta T \leq \Delta T_c \\ = 0 \quad \text{for } \Delta T > \Delta T_c \quad (10a)$$

$$T_j = \theta_t I_d V_0 + T \\ = \theta_t V_0 (c_1 - d_1 \Delta T) + \Delta T + T_0 \\ = c_2 + d_2 \Delta T \quad \text{for } \Delta T \leq \Delta T_c \\ = \Delta T \quad \text{for } \Delta T > \Delta T_c \quad (11a)$$

Again, the parameters  $c_1$ ,  $c_2$ ,  $d_1$ ,  $d_2$  are found to be positive for practical cases. A new parameter,  $T_c$ , which we shall call the cut-off temperature, is introduced here and is defined as

$$T_c - T_0 = \Delta T_c = c_1/d_1 = \frac{V_0 - V_{bo}}{\beta V_{bo}} \quad (12)$$

Equation (10) indicates that diode current decreases with elevating temperature. As the ambient temperature reaches  $T_c$ , the diode current goes to zero and remains zero for any temperature above  $T_c$ . On the other hand, the junction temperature increases with ambient temperature at a rate  $d_2$ . As the ambient temperature goes above  $T_c$ , the rate changes to unity.  $I_d$  and  $T_j$  under C-V bias are plotted against temperatures and are shown in Figs. 2 and 3.

#### Comparison of C-I and C-V Biasing

Although  $T_j$  increases with temperature when the diode has either C-I bias or C-V bias,  $T_j$  increases with temperature at a slower rate in the C-V case than in the C-I case as can be seen from the following inequality.

$$b_2 = 1 + \frac{\beta \theta_t I_0 V_{bo}}{1 - \beta \theta_t I_0 V_{bo}} > d_2 = 1 - \frac{\beta \theta_t V_0 V_{bo}}{R_{sc} + \beta \theta_t V_0 V_{bo}} \quad (13)$$

The slower rate is due to the fact that, with C-V biasing, internal heating decreases with elevating temperature. Take a commercial IMPATT diode, HP 5082-0400, for example. The diode parameters were given as follows<sup>5</sup>:

$$\beta = 1.17 \times 10^{-3}/^{\circ}\text{C} \quad V_{bo} = 76.1 \text{ V}$$

$$R_{sc} = 31 \text{ ohms} \quad V_d = 83.6 \text{ V}$$

$$\theta_t = 16^{\circ}\text{C/W} \quad I_d = 0.05 \text{ A}$$

If this diode were employed, we would have  $b_2 = 1.08$  and  $d_2 = 0.21$ . The diode junction temperature would increase with temperature at a rate five times faster with a C-I bias than with a C-V bias. The price to pay for this thermal advantage is rf output. With C-V biasing, diode current decreases with temperature at the rate of  $d_1$ . Output power, consequently, decreases at a rate of  $2d_1^2 \Delta T - 2c_1 d_1$ .

#### Experimental Results on C-V Biasing

C-V biasing was applied on a single-diode injection-locked oscillator and a twelve-diode injection-locked oscillator. The single-diode oscillator has a K-band waveguide circuit and was capable of a one-watt output. The twelve-diode oscillator has a K-band waveguide cavity combiner circuit and was capable of a 15-watt output. All IMPATT diodes used were GaAs devices. The diode current was measured as a function of temperature. The results are shown in Figs. 4 and 5. The results show a downward trend of diode current with elevating temperature, as predicted by the theory. The current cut-off point was not verified, however, as it is apparently not within the temperature range of 10°C to 50°C used in the measurements. If the situation permits, measurements will be performed with a wider temperature range in the near future. Also, tests will be performed on silicon devices to determine the applicability of the theory. It should be noticed that no change in rf performance or stability was observed when the above circuits were switched to C-I biasing.

#### Conclusion

It has been shown by analysis as well as experiment that C-V biasing can be used in IMPATT oscillator circuits and that C-V biasing offers a superior thermal property over the conventional C-I biasing. Diode junction temperature rises with ambient temperatures at a slower rate in the C-V case than in the C-I case. However, the cost of this thermal advantage is that output power drops with elevating temperature. It is not uncommon that IMPATT diodes are biased to reach their maximum junction temperature so that maximum rf power can be extracted. In cases like this, C-V biasing may be preferred so as to prevent a catastrophic failure due to thermal runaway.

#### Acknowledgment

The author is indebted to his colleague, Jeffrey Douglass, for first suggesting the use of C-V biasing.

#### References

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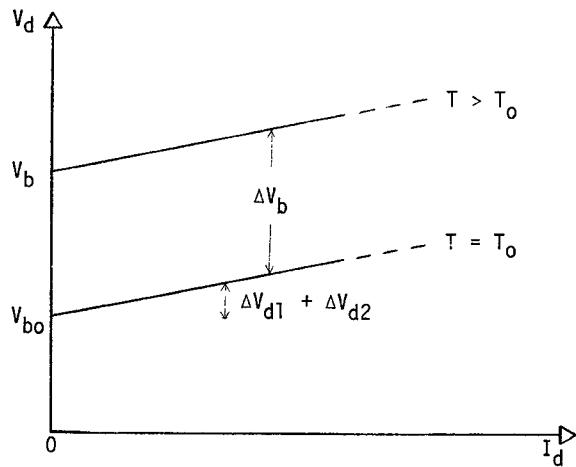


Figure 1. Diode Breakdown Voltage Characteristic

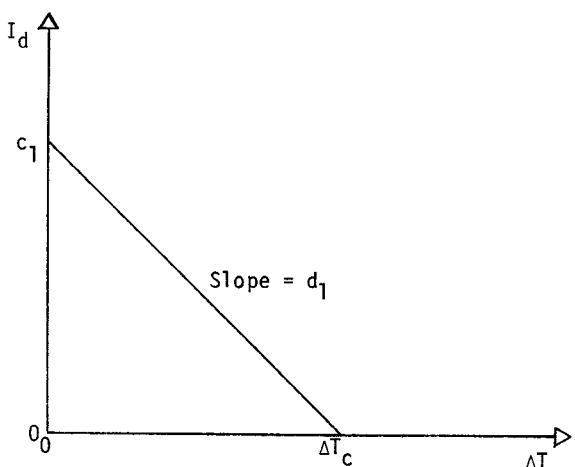


Figure 2. Diode Current vs. Temperature, C-V Bias

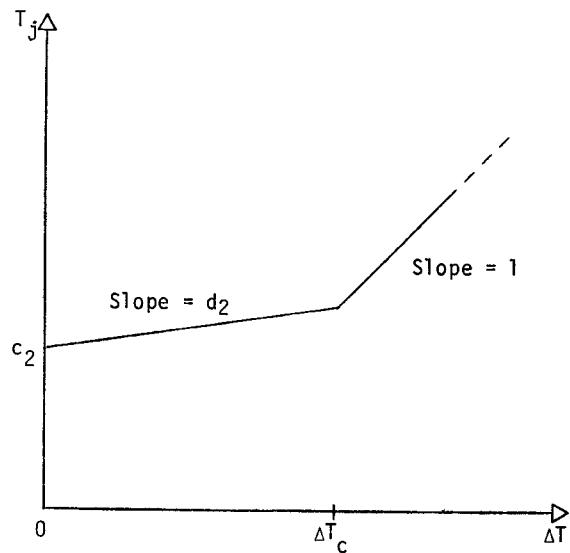


Figure 3. Diode Junction Temperature vs. Temperature, C-V Bias

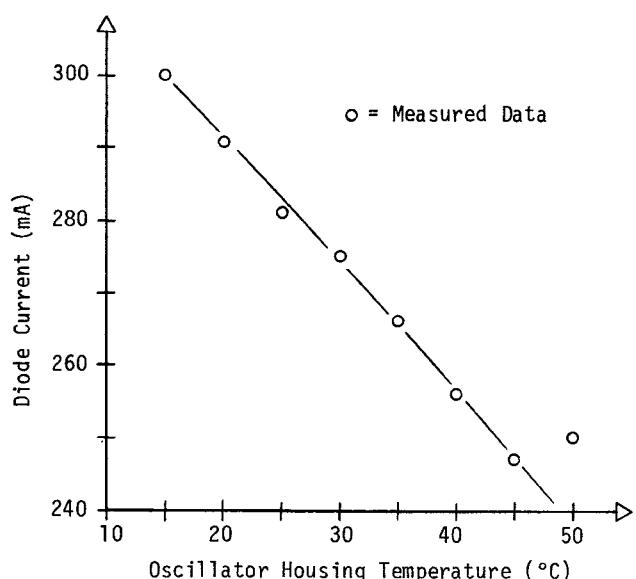


Figure 4. Thermal Property of C-V Biasing, Single-Diode Circuit

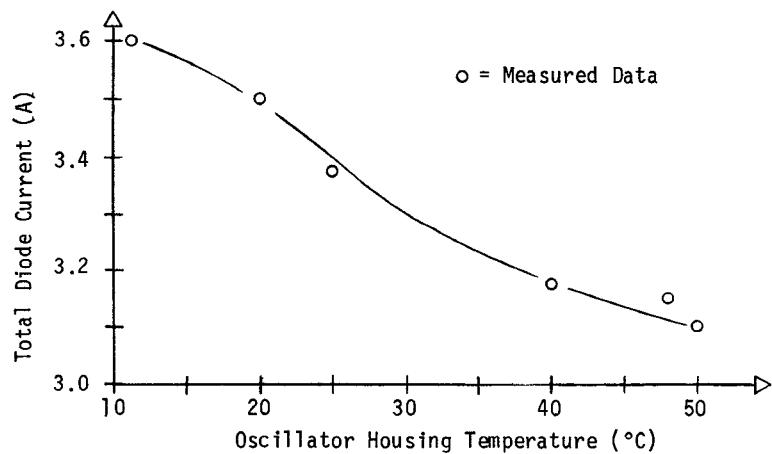


Figure 5. Thermal Property of C-V Biasing, Twelve-Diode Combiner